

**CORRIGENDA: “FINITENESS THEOREMS FOR POSITIVE  
DEFINITE  $n$ -REGULAR QUADRATIC FORMS”, TRANS. AMER.  
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ABSTRACT. This note contains a possibly incomplete list of typos found in the paper. We also include some comments to clarify a few arguments used in the proofs of the main results there.

- (1) Lemma 2.3(2): When  $\frac{dM}{4} \equiv 5 \pmod{8}$ ,  $\lambda_4(L)_2 \cong M_2^3 \perp N_2^{\frac{1}{2}}$ .
- (2) Lemma 3.1: Let  $q$  be a prime such that  $q \nmid 2k\delta$ .
- (3) Lemma 3.3: The sublattice  $M$  can be any sublattice of rank  $k < n$ . In the proof, there exists  $y \in L$  such that  $Q(y) \leq \mu_{k+1}(L)$  and  $y \notin \mathbb{Q}M$ . Then  $\delta y \in M \perp M^\perp$ . Write  $\delta y = x + z$  where  $x \in M$  and  $z \in M^\perp \setminus \{0\}$ . Therefore,  $\delta^2 \mu_{k+1}(L) \geq \delta^2 Q(y) \geq Q(z) \geq a$ .
- (4) Page 2390, at the end of first line:  $\mu_{k+1}(L) \leq C\mu_k(\ell)$ , where  $C$  is a constant depending only on  $k$ .”
- (5) Page 2390, near the end of the first paragraph of the proof of Lemma 3.4: “ $\mu_k(\tilde{K}) \leq \tilde{C}\mu_{k-1}(\tilde{K}) \leq \dots$ , where  $\tilde{C}, C_1, C_2, C_3$ , and hence  $A$ , depend only on  $\ell, L$ , and  $M$ .”
- (6) In the proof of Lemma 3.5: (1)  $q_i \in (\mathbb{Z}_p^\times)^2$  for all  $p \mid (dK)(dM)$  and  $q_i \equiv 1 \pmod{8}$ .
- (7) Section 4: The lattice  $L$  should be an  $n$ -regular lattice of rank  $n + 3$  where  $n \geq 3$  instead of  $n \geq 2$  as claimed at the beginning of that section. This is because we cannot apply Lemma 3.4 to bound  $\mu_5(L)$  in the proof of Lemma 4.1 when  $n = 2$ . However, this does not affect any subsequent arguments.
- (8) In the proof of Proposition 4.2, second paragraph: “we must have  $3p^2 \leq dM$ .”
- (9) In the proof of Proposition 4.2, third paragraph: “If  $\text{rank}(G) = k \geq 4$ , then  $p^{2(k-2)} \leq dG \leq 8(2p-2)^{k-2}$  and thus  $p$  is bounded.”

- (10) The end of the third paragraph of the proof of Lemma 4.2: “These four binaries do not represent 6, 4, 10 and 6 respectively. Therefore,  $p \leq 5$ .”
- (11) Page 2392, 2nd paragraph: One can use [1, Corollary 3.2] to bound the first three minima of  $L$ . Moreover,  $M$  is not necessary a  $4 \times 4$  section of  $L$ . It can be any quaternary sublattice of  $L$  whose discriminant is bounded.
- (12) Page 2392, proof of Theorem 1.1 ( $n = 2$ ), three lines after (2):  $N'_q$  is represented by  $L_q$ , not  $L_p$  as written.
- (13) Page 2392, proof of Theorem 1.1 ( $n = 2$ ), at the end of third paragraph: “ $\mathbb{Q}_q N'_q \not\rightarrow \mathbb{Q}_q M_q$ .”
- (14) Page 2392, proof of Theorem 1.1 ( $n = 2$ ), fourth paragraph: “ $\mu_5(L) \leq \max\{q^\alpha \mu_2(N), \mu_4(M)\}$ .”
- (15) Page 2393: Equality (1) when  $q = 2$  means that  $s$  and  $-u'v'$  are in the same square class in  $\mathbb{Z}_2^\times$ . Same comment applies to equality (2).
- (16) Page 2393, near the end of the second paragraph: “ $\mathbb{Q}_q N_q \not\rightarrow \mathbb{Q}_q M_q$ .”
- (17) Page 2393, at the end of the third paragraph: It is clear that  $\lambda_{2q}(L) = \Lambda_{2q}(L)^r$ , where  $r = \frac{1}{q}$  or  $\frac{1}{q^2}$ . Note that whenever  $\mathfrak{s}(L) = 2\mathbb{Z}$  or  $Q(L_q) \neq 2\mathbb{Z}_q$ ,  $\Lambda_{2q}(L)$  is just  $\{x \in L : Q(x) \in 2q\mathbb{Z}_q\}$  and hence  $\Lambda_{2q}(M)$  is a sublattice of  $\Lambda_{2q}(L)$ . We replace  $L$  by  $\lambda_{2q}(L)$  and  $M$  by  $\Lambda_{2q}(M)^r$  (which is not necessarily equal to  $\lambda_{2q}(M)$ ). Repeat this process until  $L_q$  is split by  $\mathbb{H}$ .
- (18) Page 2393, at the end of the fourth paragraph: Alternatively, one could argue that by assumption  $M_p$  must be represented by  $\mathbb{A} \perp \mathbb{A}^p$  and hence  $\langle a \rangle$  must be represented by  $\langle p^k \epsilon \rangle$ . Therefore,  $\text{ord}_p(a) \geq k$  and we may simply take  $\eta$  to be the smallest even integer greater than or equal to  $\text{ord}_p(a)$ .
- (19) Page 2393, last paragraph: “Let  $r \nmid 2dL$  be a prime ...”
- (20) Page 2394, first displayed inequality: “ $p^{\text{ord}_p(a)} \leq (dM)^2 \max\{2t, 2W, \mu_4(M)\}$ .”
- (21) Page 2394, after the first displayed inequality: “If  $2W \leq \max\{2t, \mu_4(M)\}$ ,”
- (22) Page 2394, second displayed inequality: “ $p^{\text{ord}_p(a)} \leq \frac{2t^2(dM)^2}{t - 2p^{\eta - \text{ord}_p(a)} r (dM)^2}$ .”
- (23) Page 2394/2395, in the proof of Theorem 1.2 and Theorem 1.3: It suffices to take  $M$  to be a ternary sublattice of  $L$  whose discriminant is bounded.

## REFERENCES

- [1] W.K. Chan, A.G. Earnest, and B.-K. Oh, *Regularity properties of positive definite integral quadratic forms*, Algebraic and arithmetic theory of quadratic forms, 59-71, Contemp. Math., **344**, Amer. Math. Soc., Providence, RI, 2004.

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